

# 第0章 数学

## 1. 傾き

$$y = ax + b$$

$$\text{傾き} = \frac{\beta}{\alpha}$$

ex.  $y = 2x + 1$

$x=1$  のとき  $y=2 \times 1 + 1 = 3$

$x=3$  のとき  $y=2 \times 3 + 1 = 7$

図 1-1

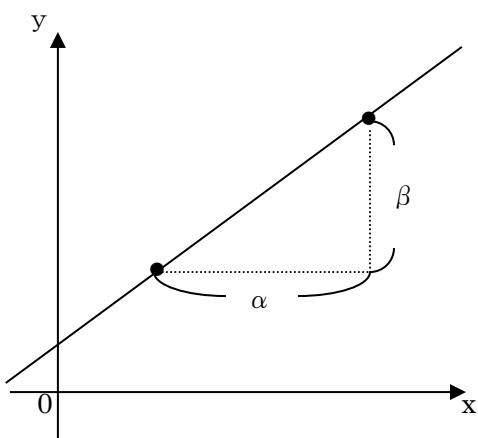
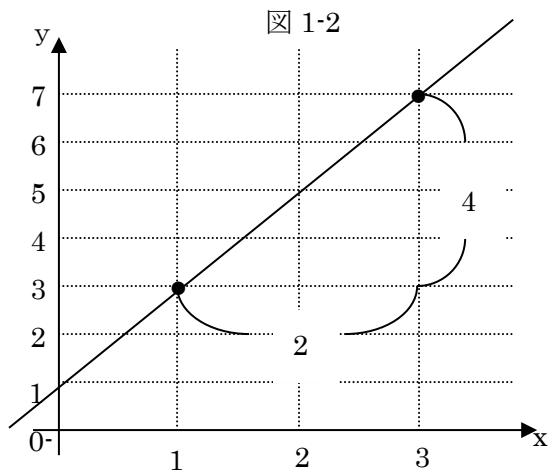


図 1-2



$$\text{傾き} = \frac{4}{2} = 2$$

## 2. 微分

### (1) 微分

・接線の傾きを求める操作

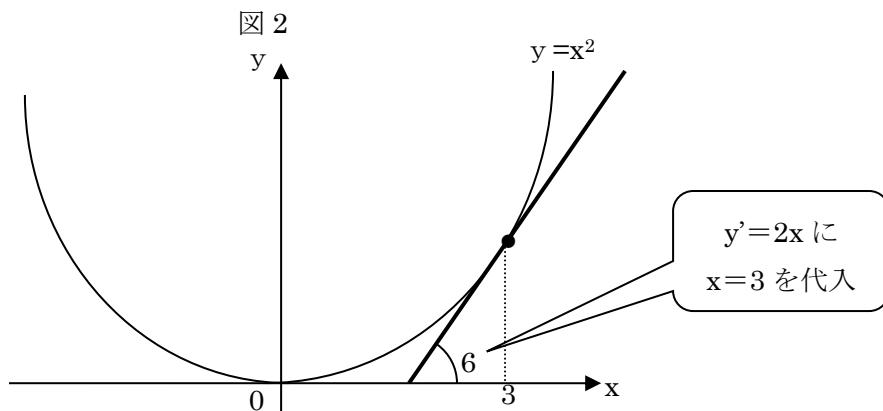
・表記法

$$y = f(x) \xrightarrow{\text{微分}} y' \text{, } f'(x)$$

### (2) 公式

$$\textcircled{1} \ y = x^n \xrightarrow{\text{微分}} y' = nx^{n-1}$$

$$\text{ex. } y = x^2 \xrightarrow{\text{微分}} y' = 2x^{2-1} = 2x$$



$$\textcircled{2} \ y = c \cdot f(x) \xrightarrow{\text{微分}} y' = c \cdot f'(x)$$

$$\text{ex. } y = 2x^3 \xrightarrow{\text{微分}} y' = 2 \cdot 3x^{3-1} = 6x^2$$

$$\textcircled{3} \ y = f(x) + g(x) \xrightarrow{\text{微分}} y = f'(x) + g'(x)$$

$$\text{ex. } y = x^5 + x^4 \xrightarrow{\text{微分}} y' = 5x^4 + 4x^3$$

$$\textcircled{4} \ y = ax \xrightarrow{\text{微分}} y' = a$$

$$\textcircled{5} \ y = c \text{ (定数)} \xrightarrow{\text{微分}} y' = 0$$

$$\text{ex. } y = 5x + 3 \xrightarrow{\text{微分}} y' = 5 + 0 = 5$$

### 3. 最大化

関数が最大



接線が水平

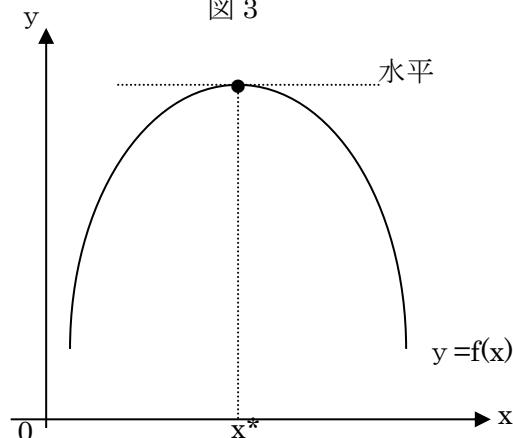


接線の傾き = 0



$$y' = 0$$

図 3



ex.  $y = -2x^2 + 8x + 1$  を最大にする  $x$  の値はいくつか。

$$y' = -2 \times 2x + 8 = -4x + 8 = 0$$

$$\therefore x = 2$$

答  $x = 2$